

Wdh

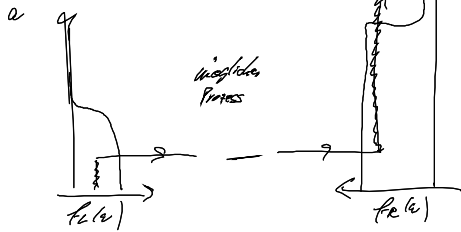
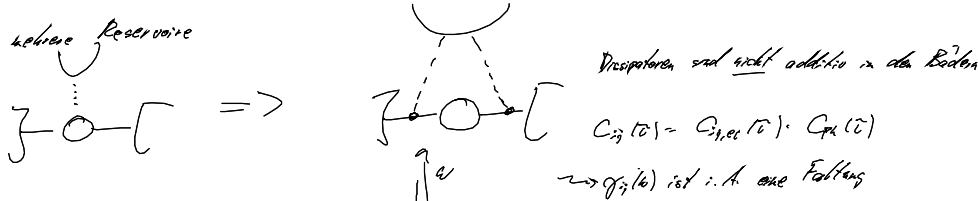
• Polaron-Hastens Wirkung

$$H = H_S + \underbrace{\sum_k (\lambda_k b_k + \lambda_k^\dagger b_k^\dagger)}_{\text{Kopplung}} + \underbrace{\sum_k \lambda_k b_k^\dagger b_k}_{\text{Band}} + \sum_k \frac{\omega_k^2}{\omega_k} S^z$$

$$H_p = \exp\left[S \sum_k \frac{\lambda_k^\dagger}{\omega_k} (b_k^\dagger - b_k)\right] \quad \text{verschiebt System- & Band-Operatoren}$$

$$H' = H_p H S H_p^\dagger = \underbrace{H_p H S H_p^\dagger}_{\text{renorm. Kopplung}} + \sum_k \lambda_k b_k^\dagger b_k \quad \rightarrow \text{Ableitung einer Standard-Hastengl.}$$

• mehrere Resonanze



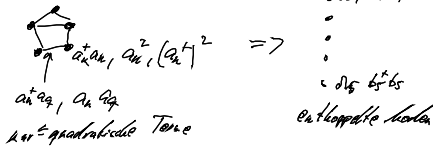
• Bogelscher Trafo (keine korrekte Ein-/Ausg., ('Quasi-Terminen'))

$$a_k = \sum_j (\lambda_{kj} b_j + \chi_{kj} b_j^\dagger) \quad k = (\lambda_{kj})$$

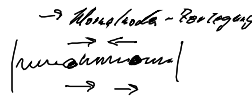
$$a_k^\dagger = \sum_j (\lambda_{kj}^\dagger b_j^\dagger + \chi_{kj} b_j) \quad V = (\chi_{kj})$$

$$\begin{cases} k V k^\dagger - V V^\dagger = \mathbb{1} \\ k V^\dagger - V^\dagger k^\dagger = \mathbb{0} \end{cases}$$

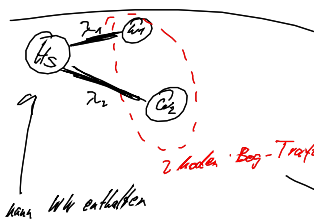
Wellenfunktion  $\rightarrow$  veränderte Kanalkonzepte



Analogon herbei: gel. Operatoren



4.3.2. 2-Ade Beispiel



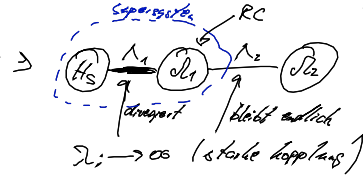
$$H = H_S + \lambda_1 \left( a_1^\dagger + \frac{\lambda_1}{\omega_1} S \right) \left( b_1 + \frac{\lambda_1}{\omega_1} S \right) + \lambda_2 \left( a_2^\dagger + \frac{\lambda_2}{\omega_2} S \right) \left( b_2 + \frac{\lambda_2}{\omega_2} S \right)$$

$$= H_S + \lambda_{11} \left( b_1^\dagger + \frac{\lambda_1}{\omega_1} S \right) \left( b_1 + \frac{\lambda_1}{\omega_1} S \right) + \lambda_{22} \left( b_2^\dagger + \frac{\lambda_2}{\omega_2} (b_1 + b_1^\dagger) \right) \left( b_2 + \frac{\lambda_2}{\omega_2} (b_1 + b_1^\dagger) \right)$$

man WK erhalten

früher Bog-Trafo so, dass

$$a_k = \sum_{j=1}^2 (\lambda_{kj} b_j + \chi_{kj} b_j^\dagger)$$



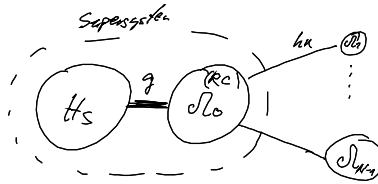
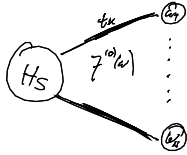
$$T_{RC} \{ \rho_{S+RC}(t) \} = \rho_S(t)$$

4.3.3. Ableitung der RC-Abbildung

$$H = H_S + \sum_k a_k (a_k^\dagger + \frac{b_k}{m} \cdot S) \quad (a_k = \frac{b_k}{m} S)$$

$$= H_S + d_0 (b^\dagger + \frac{g}{d_0} S) (b + \frac{g}{d_0} S) + \sum_k d_k (b_k^\dagger + \frac{h_k}{d_k} (b+b^\dagger)) \times (b_k + \frac{h_k}{d_k} (b+b^\dagger))$$

Kopplg:  $\tilde{Z}^{(0)}(\omega) = 2\pi \sum_k |a_k|^2 \delta(\omega - \omega_k)$   
ursprüngliche SD



$\tilde{Z}^{(1)}(\omega) = 2\pi \sum_k |h_k|^2 \delta(\omega - \omega_k)$   
residuale SD

Res.-Kopplg      Wo liegt die Residual-Bad-Eng?

$\tilde{Z}^{(0)}(\omega) \Rightarrow g, d_0, \tilde{Z}^{(1)}(\omega) ?$

Trasfo:  $a_k = m_{k0} \cdot b + \sum_{q \neq k} t_{kq} \cdot b_q$   
 $+ d_{k0} b^\dagger + \sum_{q \neq k} d_{kq} b_q^\dagger$

Koeffizientenvergleich: Terme linear in S  
 $\sum_k b_k (a_k + a_k^\dagger) \stackrel{!}{=} g (b + b^\dagger)$   
Terme quadratisch in S  
 $\sum_k \frac{b_k^2}{m} = \frac{g^2}{d_0}$

$$d_0^2 = \frac{\int_0^\infty \omega \cdot \tilde{Z}^{(0)}(\omega) d\omega}{\int_0^\infty \frac{\tilde{Z}^{(0)}(\omega)}{\omega} d\omega}$$

$$g^2 = \frac{1}{2\pi d_0} \int_0^\infty \omega \cdot \tilde{Z}^{(0)}(\omega) d\omega$$

Abb. über spektrale Dichte: finde BWGL für Operator A in System

Hessenberg-BWGL  $\tilde{A} = e^{+it} A e^{-it}$

①  $\tilde{A} = e^{+it} [H, A] e^{-it}$

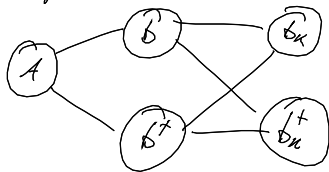
$= i \cdot \tilde{S}_1 + i \cdot \tilde{S}_2 \sum_k t_k (a_k + a_k^\dagger)$

$\tilde{S}_1 = e^{+it} [H_S + \sum_k \frac{t_k^2}{m} S^2, A] e^{-it}$   
 $\tilde{S}_2 = e^{-it} [S, A] e^{-it}$

$\dot{a}_k = -i m_k a_k - i t_k \tilde{S}$   
 $\dot{a}_k^\dagger = +i m_k a_k^\dagger + i t_k \tilde{S}$

$\Rightarrow$  eliminiere  $\tilde{a}_k$  &  $\tilde{a}_k^\dagger \rightarrow$  Gleichung für  $\tilde{A}$

② analog in 2. Bild mit  $\tilde{A}, \tilde{b}, \tilde{b}^\dagger, \tilde{b}_k, \tilde{b}_k^\dagger$



eliminiere (nach FT)  $b_k, b_k^\dagger$ , dann  $b, b^\dagger \rightarrow$  Gleichung für  $\tilde{A}$

Cauchy-Transfo von  $\tilde{Z}(\omega) \rightarrow \tilde{W}(z)$

$$\tilde{W}(z) = \frac{2}{\pi} \int_0^\infty \frac{\omega \tilde{Z}(\omega)}{z^2 - \omega^2} d\omega = \frac{1}{\pi} \int_{-\infty}^\infty \frac{\tilde{Z}(\omega)}{\omega - z} d\omega$$

$\lim_{\epsilon \rightarrow 0} \tilde{W}(z \pm i\epsilon) = \lim_{\epsilon \rightarrow 0} \frac{1}{\pi} \int_{-\infty}^\infty \frac{\tilde{Z}(\omega)}{\omega - z \pm i\epsilon} d\omega = \lim_{\epsilon \rightarrow 0} \frac{1}{\pi} \int_{-\infty}^\infty \frac{\tilde{Z}(\omega) [\omega - z \pm i\epsilon]}{(\omega - z)^2 + \epsilon^2} d\omega$  Trick

$$= \frac{1}{\pi} \mathcal{P} \int \frac{\tilde{Z}(\omega)}{\omega - z} d\omega + i \tilde{Z}(z)$$

∴ [Skript]

$$\Rightarrow f^{(1)}(\omega) = \frac{g^2 \cdot f^{(0)}(\omega)}{\left[ \frac{1}{\pi} \int \frac{f^{(0)}(\omega')}{\omega - \omega'} d\omega' \right]^2 + [f^{(0)}(\omega)]^2}$$

- $f^{(1)}(\omega) \rightarrow \alpha \cdot f^{(0)}(\omega)$   
 $g^2 \rightarrow \alpha \cdot g^2$   
 $f^{(1)}(\omega) \rightarrow f^{(0)}(\omega)$  bleibt gleich  
 $\rightarrow$  Starke Kopplung  $f^{(1)}(\omega)$  kann mit Separationsansatz behandelt werden
  - rekursive Ann. möglich
  - für SDs mit komp. Support  $f^{(1)}(\omega) = 0$   
 $\forall \omega \notin [0, \omega_m]$
- $$\bar{f}(\omega) = \omega \cdot \sqrt{1 - \frac{\omega^2}{\omega_m^2}} \quad \mathcal{O}(\omega_m^2 - \omega^2)$$
- Robin-SD

4.3.4. Ann. Spin-Boson-Modell

$$H = \frac{\epsilon}{2} b^\dagger + b^\dagger \sum_k t_k (a_k + a_k^\dagger) + \sum_k \epsilon_k a_k^\dagger a_k + \sum_k \frac{\epsilon_k^2}{\epsilon_k} \cdot \mathbb{1}$$

$$= \frac{\epsilon}{2} b^\dagger + \underbrace{d_0}_{H_0} \left( b^\dagger + \frac{2}{d_0} b^\dagger \right) \left( b + \frac{2}{d_0} b \right) + \sum_k d_k \left( b_k^\dagger + \frac{\epsilon_k}{d_k} (b + b^\dagger) \right) \left( b_k + \frac{\epsilon_k}{d_k} (b + b^\dagger) \right)$$

$H_0 \rightarrow ME$

hier: Born- & Markov-Näherung

$$\dot{\rho} = -i [H_0', \rho] + \int_0^\infty dt' \left[ C(t') \left[ (b + b^\dagger), e^{-iH_0' t'} (b + b^\dagger) e^{+iH_0' t'} \rho \right] d_0 + h.c. \right]$$

$$\int_0^\infty C(t') e^{-iH_0' t'} (b + b^\dagger) e^{+iH_0' t'} dt' = \sum_{a_0} \langle a_0 | (b + b^\dagger) | a_0 \rangle \int_0^\infty C(t') e^{-i(E_0 - E_a) t'} dt' \quad |a \times b\rangle$$

$$f^{(1)}(\omega) \left[ 1 + \chi_0(\omega) \right] = \frac{\gamma(E_0 - E_a)}{2} + \frac{i}{\pi} \int \frac{\gamma(\omega)}{E_0 - E_a - \omega} d\omega$$

Landau-Stoff  $\approx 0$

beachte •  $|\rho_{aa}\rangle = \left| \frac{1}{2} \text{Tr} \left[ (E_x + i\Gamma) \rho(t) \right] \right|$  Kohärenz

$\uparrow$   
Spara-System

$$\bullet \frac{d}{dt} \left\langle \sum_k \epsilon_k a_k^\dagger a_k \right\rangle = - \frac{d}{dt} \left\langle b^\dagger \sum_k t_k (a_k + a_k^\dagger) \right\rangle = - \frac{d}{dt} g \langle b^\dagger (b + b^\dagger) \rangle$$

für  $\rho_0 \neq \int_0^\infty \int_0^\infty \otimes \frac{e^{-\beta d_0 [b^\dagger b + b + b^\dagger]^2}}{Z_{RC}}$

