

Wdh $\sum_{\mu} Z^{(\mu)} \rho^{\pm} = -i [H_S, \rho]$

$Z = Z^{(0)} + \sum_{\mu} Z^{(\mu)}$
 Spezialfall für Resonanz \checkmark

$\sum_{\mu} \frac{e^{\beta \nu [H_S - \mu H_S]}}{Z_S} = 0$

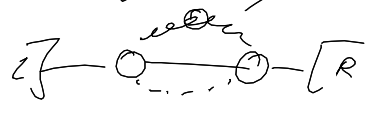
$\begin{cases} \dot{I}_E^{(\mu)} = \text{Tr}\{H_S(Z^{(\mu)}\rho)\} \\ \dot{I}_A^{(\mu)} = \text{Tr}\{H_S(Z^{(\mu)}\rho)\} \end{cases} \Rightarrow \dot{Q}^{(\mu)} \equiv \dot{I}_E^{(\mu)} - \mu \dot{I}_A^{(\mu)}$

$\Rightarrow \dot{S}_i \equiv \dot{S} - \sum_{\nu} \beta_{\nu} \dot{Q}^{(\nu)} = \dot{S} + \sum_{\nu} \dot{S}_{res}^{(\nu)} \geq 0$ 2. HS

↑
 Änderung der System-Entropie

Steady-state: $\dot{S} = 0 \Rightarrow \dot{S}_i = - \sum_{\nu} \beta_{\nu} L \dot{I}_E^{(\nu)} - \mu \dot{I}_A^{(\nu)} \geq 0$

z. Bsp.: 2-Terminal

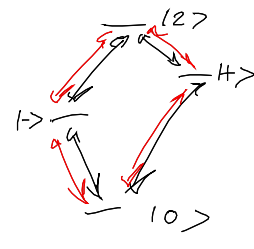


$\dot{S}_i = (\beta_R - \beta_L) \dot{I}_E + (\beta_L \mu_L - \beta_R \mu_R) \dot{I}_A \geq 0 \rightarrow$ Carnot-Beschränkungen

Bsp: SET
 DQD
 BAS: \sum_{BAS}^{PPP}



- 10 >
- 1 >
- 1+ >
- 12 >



$\rho = \begin{pmatrix} \rho_{0,0} & 0 & 0 & 0 \\ 0 & \rho_{1,1} & 0 & 0 \\ 0 & \rho_{1+} & \rho_{1+} & 0 \\ 0 & 0 & 0 & \rho_{2,2} \end{pmatrix}$

Separate Gleichung (Zerfall)

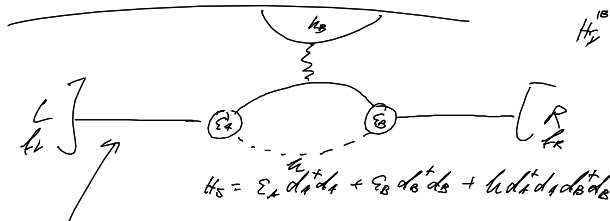
$\dot{\rho}_{1+} = \kappa \cdot \rho_{1+}$

$\text{Re}(\kappa) < 0$

$Z_{6 \times 6} = \left(\begin{array}{ccc|cc} Z_{4 \times 4} & 0 & 0 \\ \hline -0- & \kappa & 0 \\ -0- & 0 & \kappa^* \end{array} \right)$

Blockstruktur gilt nur für well unterteilt Systeme

2.7. Phonon-assistiertes Tunneln



$$H_T^{(B)} = (d_A^\dagger d_B + d_B^\dagger d_A) \otimes \sum_k (k_A b_k + k_B b_k^\dagger)$$

- 100 > : 0 Anstiege (obdA)
- 110 > : \epsilon_A \epsilon_A < \epsilon_B
- 101 > : \epsilon_B
- 111 > : \epsilon_A + \epsilon_B + \epsilon

$$H_L^{(A)} = \sum_k (t_{kL} c_{kL}^\dagger \cdot d_A + h.c.)$$

$$\sum_L^{pop} = \Gamma_L \begin{pmatrix} -f_L(\epsilon_A) & 1-f_L(\epsilon_A) & 0 & 0 \\ f_L(\epsilon_A) & -[1-f_L(\epsilon_A)] & 0 & 0 \\ 0 & 0 & -f_L(\epsilon_B) & 1-f_L(\epsilon_A+\epsilon_B) \\ 0 & 0 & f_L(\epsilon_A+\epsilon_B) & -[1-f_L(\epsilon_A+\epsilon_B)] \end{pmatrix}$$

$$\Gamma_L(\epsilon) \approx \Gamma_V$$

analog \sum_R^{pop}

$$\sum_B^{pop} = \Gamma \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & -f_B(\epsilon_B) & 1+f_B(\epsilon_B-\epsilon_A) & 0 \\ 0 & f_B(\epsilon_B-\epsilon_A) & -[1+f_B(\epsilon_B-\epsilon_A)] & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$k_B(\epsilon_B - \epsilon_A) = \frac{1}{e^{\beta_B(\epsilon_B - \epsilon_A)} - 1}$$

$$\sum^{pop} = \sum_L^{pop} + \sum_R^{pop} + \sum_B^{pop}$$

BAS: Ströme zu SS

$$\dot{S}_i \geq 0 \quad \dot{S}_i = -\beta_B \bar{I}_E^{(B)} - \beta_L \left[\bar{I}_E^{(L)} - \beta_L \bar{I}_A^{(L)} \right] - \beta_R \left[\bar{I}_E^{(R)} - \beta_R \bar{I}_A^{(R)} \right] \geq 0$$

$$\begin{aligned} \bar{I}_A &= \bar{I}_A^{(L)} = -\bar{I}_A^{(R)} \\ \bar{I}_E^{(L)} + \bar{I}_E^{(R)} + \bar{I}_E^{(B)} &= 0 \end{aligned}$$

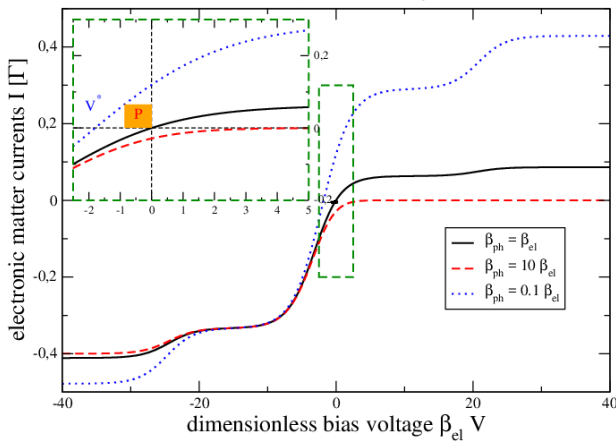
$$\dot{S}_i = (\beta_R - \beta_B) \bar{I}_E^{(B)} + (\beta_R - \beta_L) \bar{I}_E^{(L)} + (\beta_L \beta_L - \beta_R \beta_R) \bar{I}_A^{(L)}$$

tight-coupling: $\bar{I}_E^{(B)} = (\epsilon_B - \epsilon_A) \cdot \bar{I}_A^{(L)}$

Fall: $\beta_B = \beta_L = \beta_{oc} + \beta_B$

$$\rightarrow \dot{S}_i = \left\{ [\beta_{oc} - \beta_B] \cdot (\epsilon_B - \epsilon_A) + \beta_{oc} (\beta_L - \beta_R) \right\} \bar{I}_A^{(L)} \geq 0$$

bei $V = \frac{\mu_c^* - \mu_a^*}{e} = \left(\frac{1e_c}{1e_a} - 1\right) (e_0 \cdot \text{sr})$ Verschiebung des Stroms



$$\bar{P} = -(\mu_c - \mu_a) \bar{I}_a^{(c)}$$

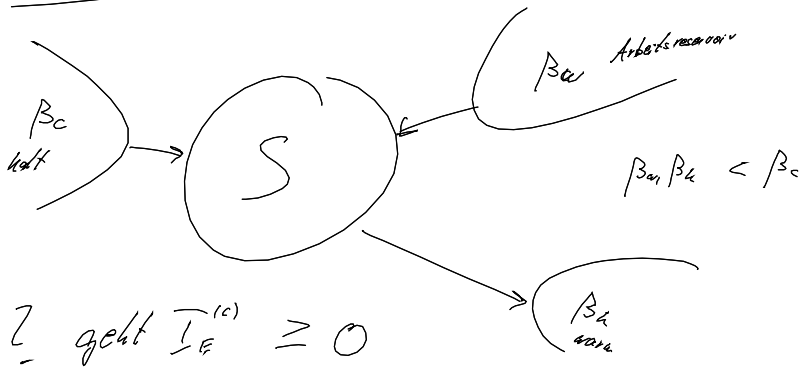
$$\eta = \frac{-(\mu_c - \mu_a) \cdot \bar{I}_a^{(c)} \cdot \Theta(P)}{\dot{Q}_{in}}$$

a) $\frac{\mu_B}{T_B} > \frac{\mu_c}{T_c} \Leftrightarrow 1 - \frac{T_c}{T_B} \left. \vphantom{\frac{\mu_B}{T_B}} \right\} \equiv \dot{Q}_c$

b) $\frac{\mu_B}{T_B} < \frac{\mu_c}{T_c} \Leftrightarrow 1 - \frac{T_B}{T_c} \left. \vphantom{\frac{\mu_B}{T_B}} \right\} \equiv \dot{Q}_c$

$$\dot{Q}_{in} = \dot{Q}^{(c)} + \dot{Q}^{(a)}$$

2.8. Machbarkeit des Kollens mit 3 Terminal-Systemen



$$\text{2. HS: } \underbrace{(\beta_u - \beta_c)}_{\leq 0} \underbrace{\bar{I}_E^{(c)}}_{\geq 0} + \underbrace{(\beta_u - \beta_a)}_{\geq 0} \cdot \bar{I}_E^{(a)} \geq 0 \quad \text{aus } \bar{I}_E^{(a)} = -(\bar{I}_E^{(c)} + \bar{I}_E^{(a)})$$

$$\implies \beta_c > \beta_a > \beta_u$$

Wann geht das?

1. Versuch: 2 levels $E_0 < E_1$

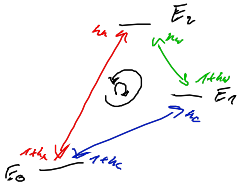
$$\sum_z \Gamma_z = \Gamma_c \begin{pmatrix} -\hbar\omega & 1 + \hbar\omega \\ \hbar\omega & -(1 + \hbar\omega) \end{pmatrix} + \Gamma_h \begin{pmatrix} -\hbar\omega & 1 + \hbar\omega \\ \hbar\omega & -(1 + \hbar\omega) \end{pmatrix} + \Gamma_u \begin{pmatrix} -\hbar\omega & 1 + \hbar\omega \\ \hbar\omega & -(1 + \hbar\omega) \end{pmatrix}$$

$$k_v = \frac{1}{e^{\beta_v(E_v - E_0)} - 1}$$

$$\leadsto \bar{p}_0 = \frac{1 + \bar{k}}{1 + 2\bar{k}}, \quad \bar{p}_1 = \frac{\bar{k}}{1 + 2\bar{k}}; \quad \bar{h} = \frac{\Gamma_c \cdot k_c + \Gamma_h \cdot k_h + \Gamma_v \cdot k_v}{\Gamma_c + \Gamma_h + \Gamma_v} > k_c$$

\leadsto Kälte geht nicht \bar{v}

2. Versuch: 3 level



$$E_0 < E_1 < E_2$$

$$\sum_3^{PP} = \begin{pmatrix} -\Gamma_c k_c - \Gamma_h k_h & \Gamma_c (1 + k_c) & 0 \\ \Gamma_c k_c & -\Gamma_c (1 + k_c) & 0 \\ \Gamma_h k_h & 0 & -\Gamma_h (1 + k_h) - \Gamma_v (1 + k_v) \end{pmatrix}$$

$$k_h = \frac{1}{e^{\beta_h(E_h - E_0)} - 1}$$

$$k_c = \frac{1}{e^{\beta_c(E_c - E_0)} - 1}$$

$\leadsto k_c > k_h$ ist möglich trotz $\beta_c > \beta_h$

$$\bar{J}_E^{(1)} = \text{Tr} \left\{ H_S \left(\sum_3^{PP} \bar{p} \right) \right\}$$

$$H_S = \begin{pmatrix} E_0 & 0 & 0 \\ 0 & E_1 & 0 \\ 0 & 0 & E_2 \end{pmatrix}$$

$$\lim_{k_h \rightarrow \infty} \bar{J}_E^{(1)} = (E_1 - E_0) \frac{\Gamma_c \cdot \Gamma_h (k_c - k_h)}{\Gamma_c (1 + 3k_c) + \Gamma_h (1 + 3k_h)} \geq 0$$

gilt wenn $\beta_h (E_2 - E_0) < \beta_c (E_1 - E_0)$

analog $\bar{J}_E^{(2)} = (E_2 - E_0) \left(\dots \right)$

$$\text{COP} = \frac{E_1 - E_0}{E_2 - E_0} \otimes (k_c - k_h) \leq \frac{T_c}{T_h - T_c} = \text{COP}_{ca}$$