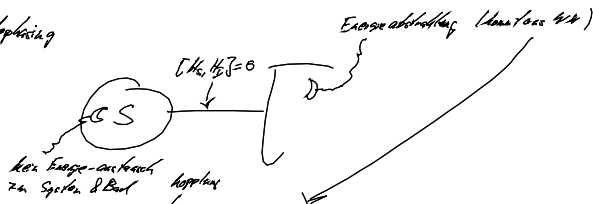


Wdh

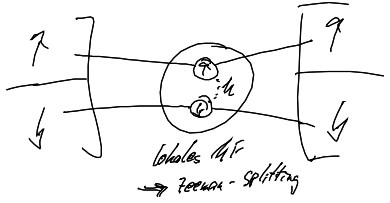
o pure depolarizing



$$\langle \mathcal{E} \rangle = \frac{z}{2} \int_0^\infty \frac{\Gamma(u)}{u} \sin^2\left(\frac{u\mathcal{E}}{2}\right) du$$

dgh. coarse-graining + ZF $\rightarrow \rho(z, t) = e^{z\hat{L}t} \rho_0 \rightarrow$ reproduz. die exakte Lösung (nur für pure-depolarizing)

o Spm-entgeltendes Zählen $\hat{O} = S = \sum_k (C_{k+}^+ C_{k+} - C_{k-}^+ C_{k-})$



$$\rightarrow Z(z) \rightarrow \bar{I} = -i \text{Tr} \{ Z'(0) \bar{\rho} \}$$

\rightarrow Spm-entgeltend

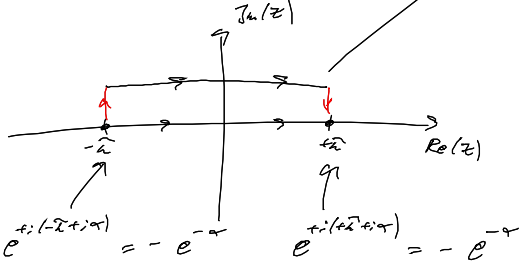
3.5. Spm-entgeltend in der FCS

3.5.1. Mathem. Einführung

$$P_n(t) = \frac{1}{2\pi} \int_{-\pi}^{\pi} A(z, t) e^{-inz} dz = \frac{1}{2\pi} \int_{-\pi}^{\pi} e^{C(z, t) - inz} dz$$

sei $C(-z, t) = C(z + i\pi, t)$

$$\frac{P_n(t)}{P_{-n}(t)} = \frac{\int_{-\pi}^{\pi} A(z, t) e^{-inz} dz}{\int_{-\pi}^{\pi} A(z, t) e^{+inz} dz} = \frac{\int_{-\pi}^{\pi} e^{C(z, t) - inz} dz}{\int_{-\pi}^{\pi} e^{C(-z, t) - inz} dz} = \frac{\int_{-\pi}^{\pi} e^{C(z, t) - inz} dz}{\int_{-\pi}^{\pi} e^{C(z, t) - inz} dz} = e^{+4 \cdot \pi}$$



$$C(-z, t) = C(z + i\pi, t) \Rightarrow \frac{P_n(t)}{P_{-n}(t)} = e^{+4 \cdot \pi}$$

Bsp: SET

$$\mathcal{Z}(z) = \Gamma_L \begin{pmatrix} -f_L & +(1-f_L)e^{-iz} \\ f_L \cdot e^{iz} & -(1-f_L) \end{pmatrix} + \Gamma_R \begin{pmatrix} -f_R & +(1-f_R) \\ +f_R & -(1-f_R) \end{pmatrix}$$

Subtrahiere $\mathbb{E} \cdot$ $\frac{|\mathcal{Z}(z) - \mathcal{Z}(z) \cdot \mathbb{E}|}{D(z)} = 0$

$$\Rightarrow D(-z) = D(+z + i \cdot \ln \left[\frac{f_L(1-f_R)}{(1-f_L) \cdot f_R} \right]) = D(+z + i \cdot [(\beta_R - \beta_L) \mathbb{E} + (\beta_L f_L - \beta_R f_R)])$$

$$\Rightarrow \mathcal{Z}_{\text{alt}}(-z) = \mathcal{Z}_{\text{alt}}(+z + i \cdot \tau) = \lim_{t \rightarrow \infty} \frac{C(x, t)}{t} \quad \text{oder} \quad \mathcal{Z}_{\text{alt}}(0) = 0$$

$$\lim_{t \rightarrow \infty} \frac{P_{nk}(t)}{P_n(t)} = e^{i \cdot [(\beta_R - \beta_L) \mathbb{E} + (\beta_L f_L - \beta_R f_R)]} \quad \leftarrow \text{integrierte Erzeugendefunktionsreihe}$$

von links nach rechts

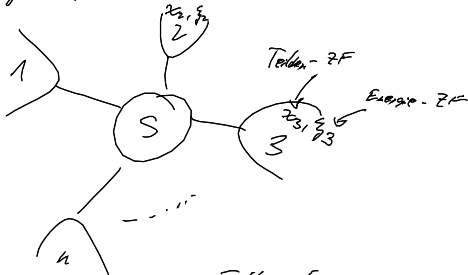
F-Theorem
"universell" gültig!

wir hatten $\ln \hat{S}_i = (\beta_R - \beta_L) \cdot \bar{I}_E + (\beta_L f_L - \beta_R f_R) \cdot \bar{I}_n$

allg.: $\frac{P(+\Delta; S)}{P(-\Delta; S)} = e^{+\Delta; S}$

$P(\pm; S) \stackrel{!}{=} \text{WS für Trajektorie mit EP } \pm; S$

- für SET: "light crossing": $\bar{I}_E = \bar{e} \cdot \bar{I}_n$
- allg.: n-terminal-System



$\Rightarrow 2n$ Zählfelder
Gesamtenergieerhaltung
"TZ-Erhaltung"

Z4-Z ZF sind wichtig

$$\hookrightarrow \dot{P} = W(x, \underline{g}) P$$

$$\left| W^T(-x-iA, -\underline{g}-iB) = W(x, \underline{g}) \right|$$

$$\underline{B} = \begin{pmatrix} \beta_1 \\ \vdots \\ \beta_n \end{pmatrix} \quad \underline{A} = - \begin{pmatrix} \alpha_1 \beta_1 \\ \vdots \\ \alpha_n \beta_n \end{pmatrix} \quad \text{"Affinitäten"}$$

$$\left| W(x, \underline{g}) - \mathcal{Z}(x, \underline{g}) \cdot \mathbb{E} \right| = 0$$

$$= \left| W(x-iA, -\underline{g}-iB) - \mathcal{Z}(x-iA, -\underline{g}-iB) \cdot \mathbb{E} \right|$$

$$= \left| W^T(-x-iA, -\underline{g}-iB) - \mathcal{Z}(-x-iA, -\underline{g}-iB) \cdot \mathbb{E} \right|$$

$$= \left| W(x, \underline{g}) - \mathcal{Z}(-x-iA, -\underline{g}-iB) \cdot \mathbb{E} \right|$$

(EW sind inv. unter Transponieren)

$$\Rightarrow \lim_{t \rightarrow \infty} C(-x-iA, -y-jB, t) = \lim_{t \rightarrow \infty} C(x, y, t)$$

$$\rightarrow \lim_{t \rightarrow \infty} \frac{P_{+A, +\Delta E}(t)}{P_{-A, -\Delta E}(t)} = e^{-\frac{(\Delta E \cdot B + \Delta N \cdot A)}{k_B T}} = e^{-\sum_N \Pr(\Delta E_N - \Delta N \cdot \mu)}$$

isolierte EP-Rate
↓

$$\frac{P_{+A, S}}{P_{-A, S}} = e^{z_1 S}$$

Crooks Fluktuationstheorem

4. Transport bei starker Kopplung

bisher $H_I \rightarrow 0$ (ME wird gut)

$$\Rightarrow \bar{p}_S = \frac{e^{-\beta(H_S - \mu N_S)}}{Z_S}$$

Thermalisierung

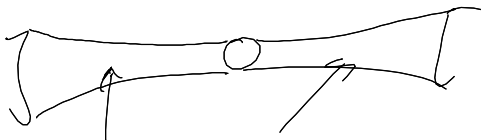
$$\dot{S}_i = \frac{d}{dt} S_{out}(t) - \sum_N \Pr[\bar{I}_E^{(N)} - \bar{I}_A^{(N)}] \geq 0$$

$$\frac{P_{+A, S}}{P_{-A, S}} = e^{+z_1 S}$$

stoch. Formulierung des 2. HS

jetzt H_I endlich

4.1 Exakt lösbares Modell: Das Fermi-Hubbard-Modell (SET, exakt)



Starke Kopplung

$$H_S = \sum d^\dagger d \quad H_B = \sum_n \epsilon_{nL} C_{nL}^\dagger C_{nL} + \sum_n \epsilon_{nR} C_{nR}^\dagger C_{nR}$$

$$H_I = \sum_n (t_{nL} d^\dagger C_{nL}^\dagger + h.c.) + \sum_n (t_{nR} d^\dagger C_{nR}^\dagger + h.c.)$$

$$H = H_S + H_I + H_B$$

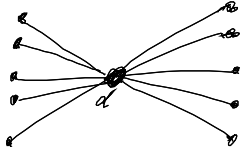
H ist eine quadrat. Form aus Erzeugern & Vernichtern

\Rightarrow exakte Lösung ist möglich analog zum Single res. Level (nur bei 2 Bändern)

→ Hermitische Gleichungen

$$\dot{\vec{d}} = e^{+i\omega t} [H_0 \vec{d}] e^{-i\omega t} = e^{+i\omega t} \left(-\varepsilon \vec{d} + \sum_k t_{kv}^* C_{kv} + t_{vk}^* C_{kv} \right) e^{-i\omega t}$$

$$\boxed{\begin{aligned} \vec{d} &= -i\varepsilon \vec{d} + i \sum_k (t_{kv}^* C_{kv} + t_{vk}^* C_{kv}) \\ \dot{C}_{kv} &= -i\varepsilon_{kv} C_{kv} + i t_{kv} \vec{d} \end{aligned}} \quad \text{ist gelöst}$$



∴ [Skript]

→ stat. Bewertung des dots

$$\bar{n} = \lim_{t \rightarrow \infty} \langle n^+ d \rangle = \int_{-\infty}^{+\infty} d\omega \frac{\Gamma_L \Gamma_R f_L(\omega)}{\Gamma_L + \Gamma_R} \stackrel{Z}{=} \frac{\Gamma_L + \Gamma_R}{(\Gamma_L^2 + \Gamma_R^2 - 4(\omega - \varepsilon)^2)}$$

Unidirekt. bias $\Gamma_L(\omega) = 2\pi \sum_k (t_{kv})^2 \delta(\omega - \varepsilon_{kv}) \approx \Gamma_L$

$$\delta(x) = \lim_{\varepsilon \rightarrow 0} \frac{1}{\varepsilon} \frac{\varepsilon}{x^2 + \varepsilon^2}$$

für schwache Kopplung gilt $\bar{n} \rightarrow \frac{\Gamma_L \cdot f_L(\varepsilon) + \Gamma_R \cdot f_R(\varepsilon)}{\Gamma_L + \Gamma_R} \stackrel{!}{=} \text{Lösung von SET}$

o inf. bias $f_L(\omega) \rightarrow 1$
 $f_R(\omega) \rightarrow 0$ $\bar{n} \rightarrow \frac{\Gamma_L}{\Gamma_L + \Gamma_R}$ (Mastergleichung wird exakt für inf. bias)

Stat. Strom

$$\bar{I}_M = \lim_{t \rightarrow \infty} \frac{d}{dt} \langle \sum_k C_{kv}^+ C_{kv} \rangle = - \lim_{t \rightarrow \infty} \frac{d}{dt} \langle \sum_k C_{kv} C_{kv} \rangle$$

∴ [Skript]

$$\bar{I}_M = \frac{\Gamma_L \Gamma_R}{\Gamma_L + \Gamma_R} \int d\omega [f_L(\omega) - f_R(\omega)] \frac{1}{\Gamma_L + \Gamma_R} \frac{(\Gamma_L + \Gamma_R)/2}{(\omega - \varepsilon)^2 + (\frac{\Gamma_L + \Gamma_R}{2})^2}$$

$$\bar{I}_{SET} = \frac{\Gamma_L \cdot \Gamma_R}{\Gamma_L + \Gamma_R} [f_L(\varepsilon) - f_R(\varepsilon)]$$

$\Gamma_L + \Gamma_R \rightarrow 0: \delta(\omega - \varepsilon)$

Landauer-Formel

$$\bar{I}_M = \frac{1}{2\pi} \int d\omega T(\omega) [f_L(\omega) - f_R(\omega)]$$

$$\bar{I}_E = \frac{1}{2\pi} \int d\omega w \cdot T(\omega) [f_L(\omega) - f_R(\omega)]$$

$$\left. \begin{aligned} & (\beta_R - \beta_L) \bar{I}_E + (\beta_L \mu_L - \beta_R \mu_R) \cdot \bar{I}_M \geq 0 \\ & \text{2. HS gilt} \end{aligned} \right\}$$

